

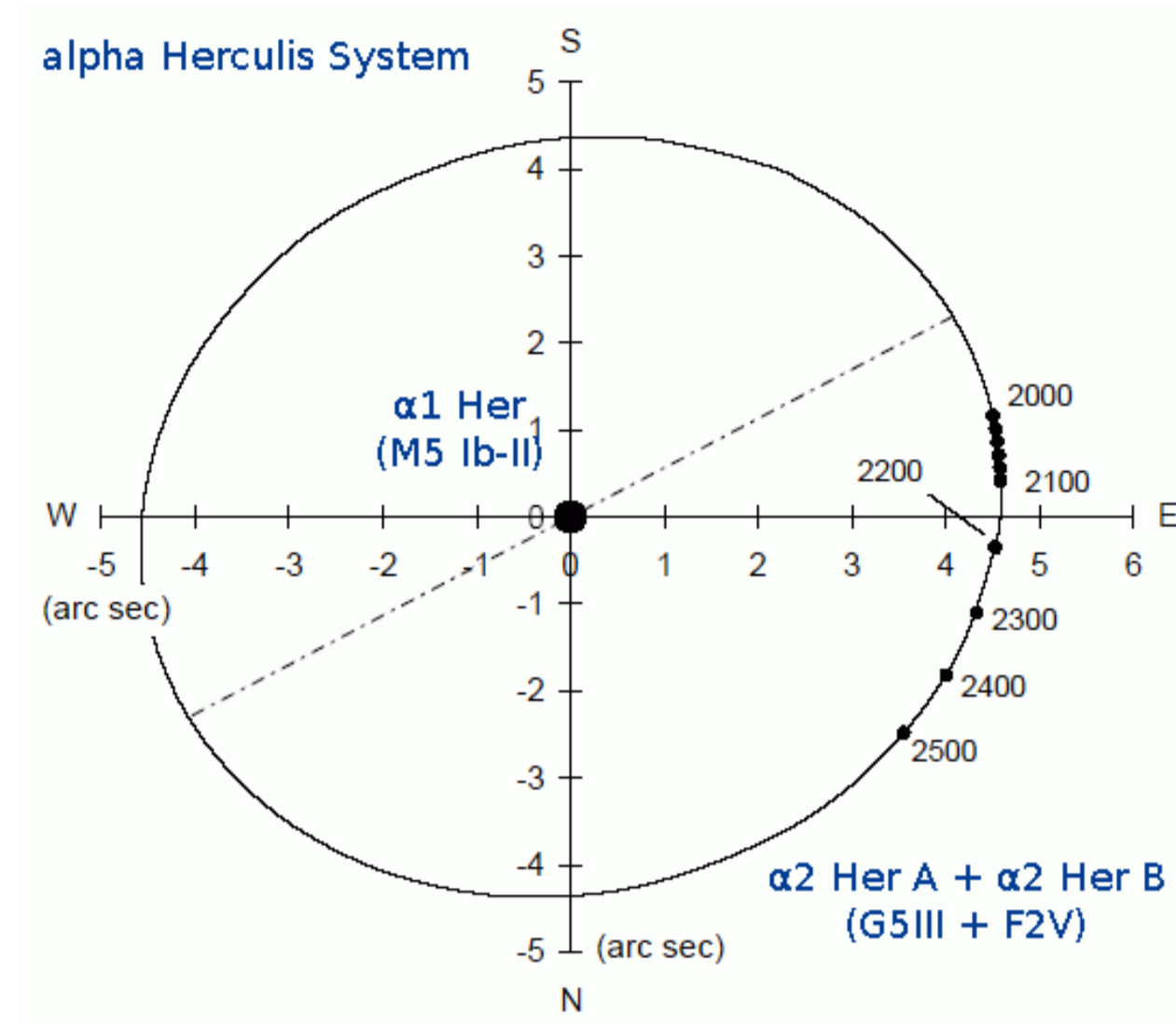
Modeling The Triple System α Herculis: Estimation of Primary AGB Star Mass

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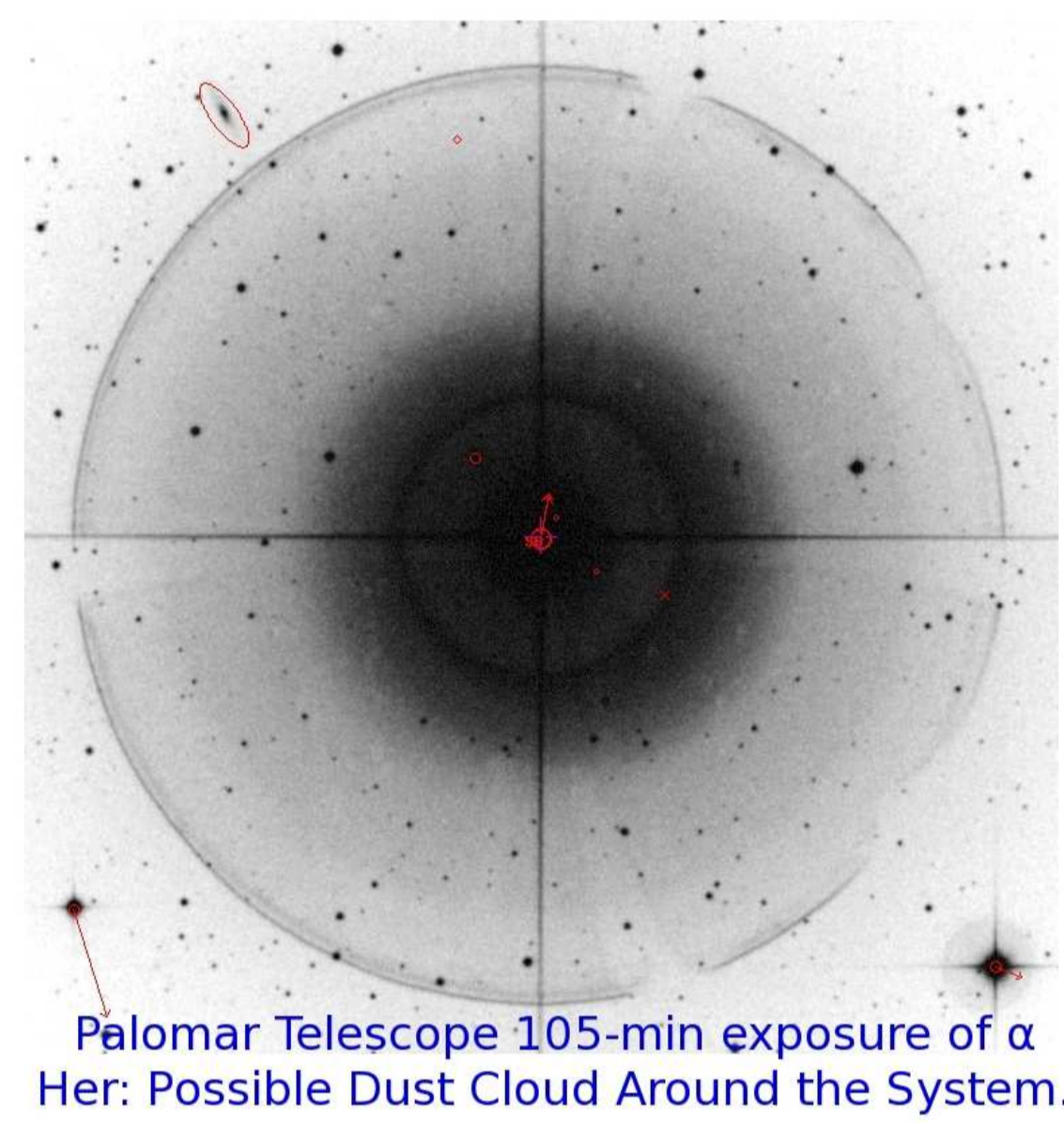
Introducing α Herculis System

- α Herculis is a *triple* stellar system. The primary α^1 Her (M5 Ib-II) and the secondary α^2 Her form a visual binary of separation $\tilde{\alpha} \approx 4.7''$, and orbital period of $P \approx 3600$ yr. The primary is an AGB star while the secondary is a spectroscopic binary itself (α^2 Her A, B).
- The distance derived from Hipparcos parallax is $d_{\text{Hip}} = 110 \pm 16$ pc, so the projected semi-major axis between α^1 Her and α^2 Her is ~ 520 AU.



Why Do We Care About α^1 Her?

- Bright** ($m_v = 3.5$ mag), nearby ($d_{\text{Hip}} = 110$ pc) AGB star,
- Controversy in the literature around its **mass** ranges from 1.7 to $17 M_{\odot}$,
- The first star whose mass loss rate was measured ($\dot{M} = 3 \times 10^{-7} M_{\odot} \text{yr}^{-1}$) [8],
- Stochastically excited **pulsations** like Red Giants (around $\Pi = 126$ d) [5],
- Long Secondary Period** ($\Pi_{\text{LSP}} \approx 1400$ d),



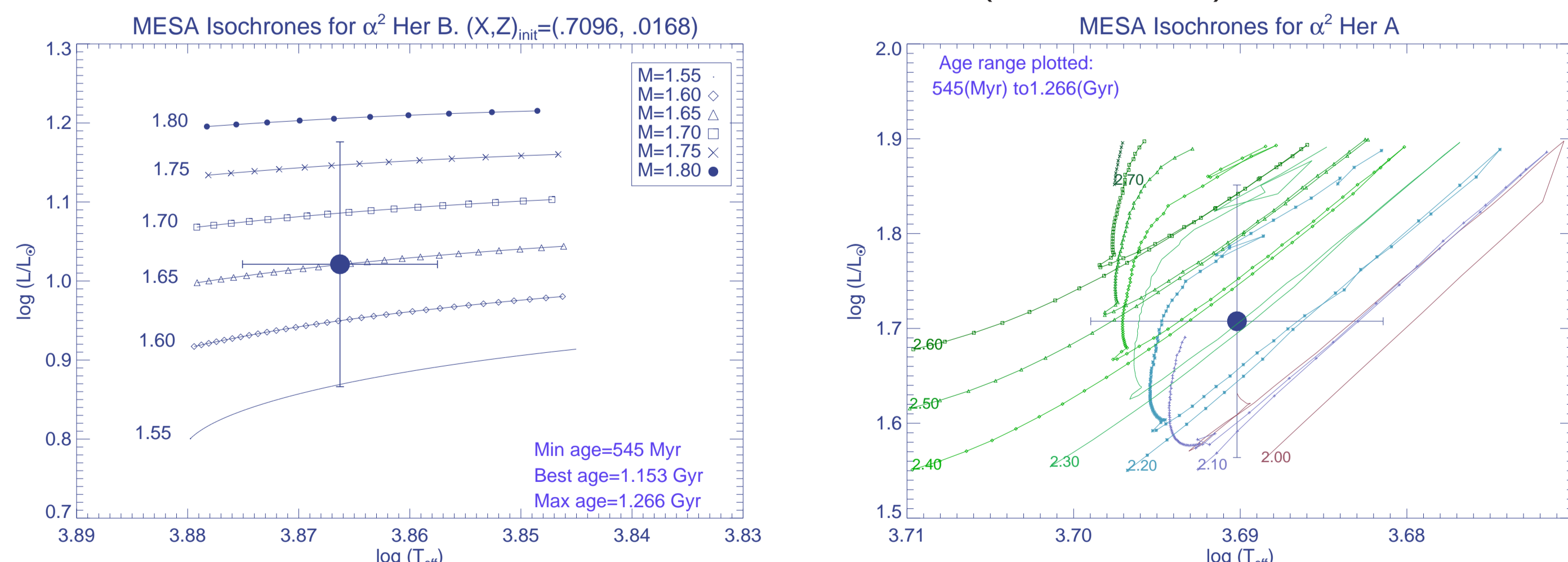
- We are interested in the pulsations of this star, and deriving its physical properties from modeling the internal structure.**
- Here is our first assessment of α^1 Her mass, based on three independent methods: (1) from $\log g$ with radii coming from Wing C calibration [5, 8], (2) from an age constraint and isochrone fitting [4], (3) from extending the asteroseismic mass and radius determination from red giants to semi-regular pulsating stars [3].
- Observations:** We have more than two decades of VRI and Wing ABC photometry carried out at Villanova University and Tennessee State University, starting from March 1986. The maximum of peak-to-peak light variability in V, for instance, is 0.98 mag, typical of an **SRC** pulsating star.

Table 1. Physical Properties of the System

| | α^1 Her | α^2 Her A | α^2 Her B | Reference |
|------------------------|-----------------|------------------|------------------|-----------|
| Spec. Class | M5 Ib-II | G8 III | A9 IV-V | [8] |
| T_{eff} [K] | 3270 ± 65 | 4900 ± 100 | 7350 ± 150 | [5], [8] |
| $\log(L/L_{\odot})$ | 3.92 ± 0.30 | 1.71 ± 0.39 | 1.02 ± 0.43 | [5] |
| $\log(g/g_{\odot})$ | -4.27 | -2.1 | -0.11 | [8] |
| Mass [M_{\odot}] | see Table 2 | 2.30 ± 0.20 | 1.65 ± 0.10 | this work |
| Radius [R_{\odot}] | 286 ± 31 | | | [5] |

Masses of Individual Members

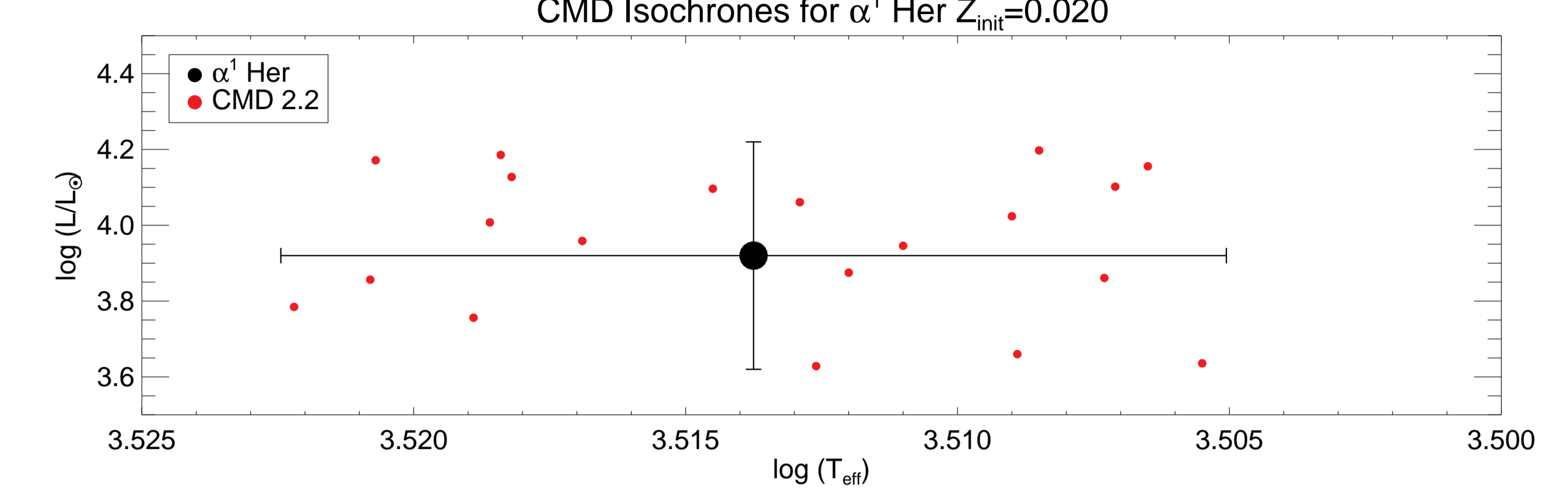
- Based on observed $\log L/L_{\odot}$ and $\log g/g_{\odot}$ (Thiering and Reimers 1993) we locate α^2 Her A and B on the HR diagram, with MESA evolutionary tracks [6], and look for the possible ranges of mass and age (see Table 1).



- Q: What is the allowed **age** and **mass** of binary companions?
A: The best age is $\tau_2 = 1.15$ Gyr, and the total mass of the binary is $m_2 = 3.95 \pm 0.30 M_{\odot}$.
- From binary system membership, it is unclear that α^1 Her is a *low-mass AGB* or a *super-AGB* star. The reason is large uncertainties in $\tilde{\alpha}$, d_{Hip} , and P .
- Assuming** that all three stars are **coeval**, forming from the same contracting cloud, then $\tau_1 \simeq \tau_2$. Based on this *age constraint*, and **CMD 2.2** isochrones for models meeting conditions in Table 1, α^1 Her mass is $2.1 \lesssim m_1 \lesssim 3.0 M_{\odot}$.

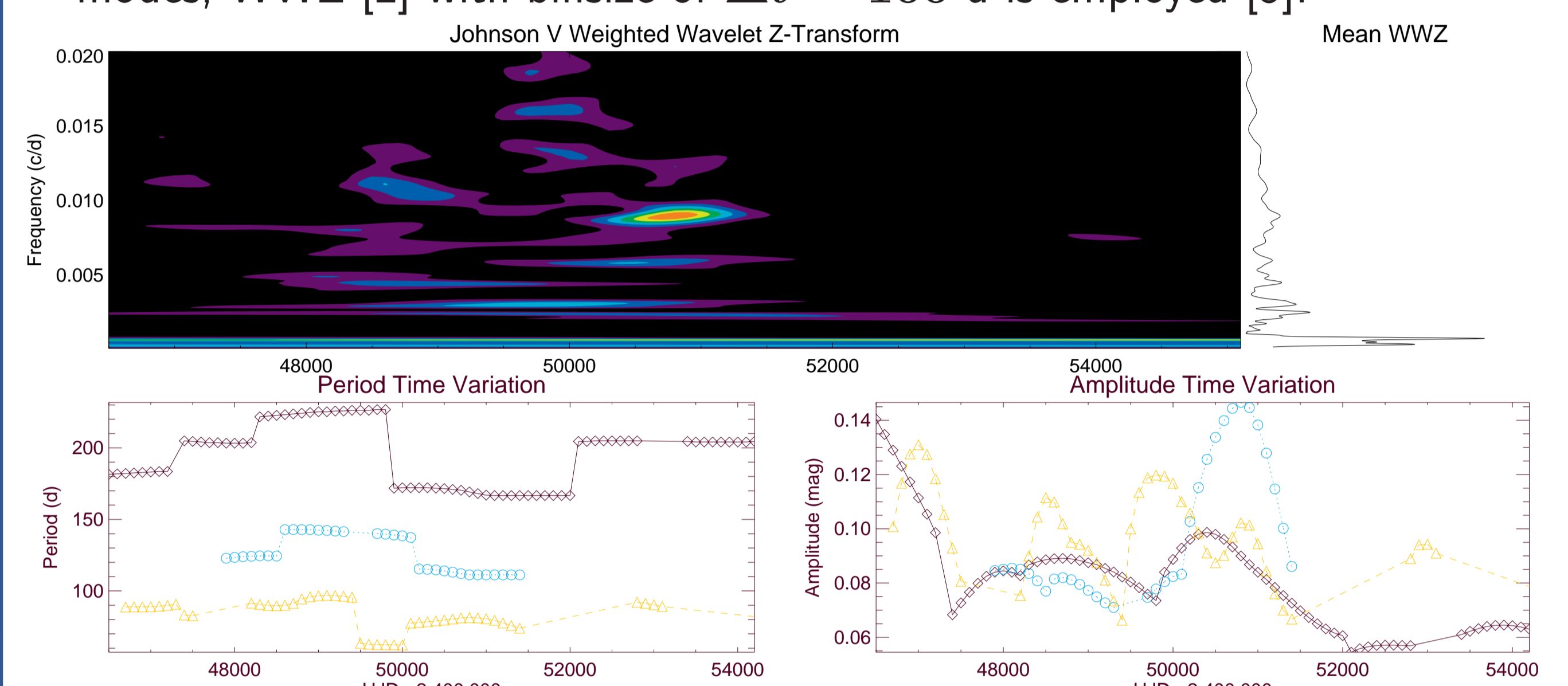
CMD 2.2 Isochrones and α^1 Her on HR Diagram

A zoomed-in view of HRD and selected CMD 2.2 isochrones (see Table 1, 2, [4]).



Semi-Regularity and Weighted Wavelet Z-Transform (WWZ)

- To demonstrate the temporal change in frequency and amplitude of three selected modes, WWZ [2] with binsize of $\Delta t = 100$ d is employed [5].

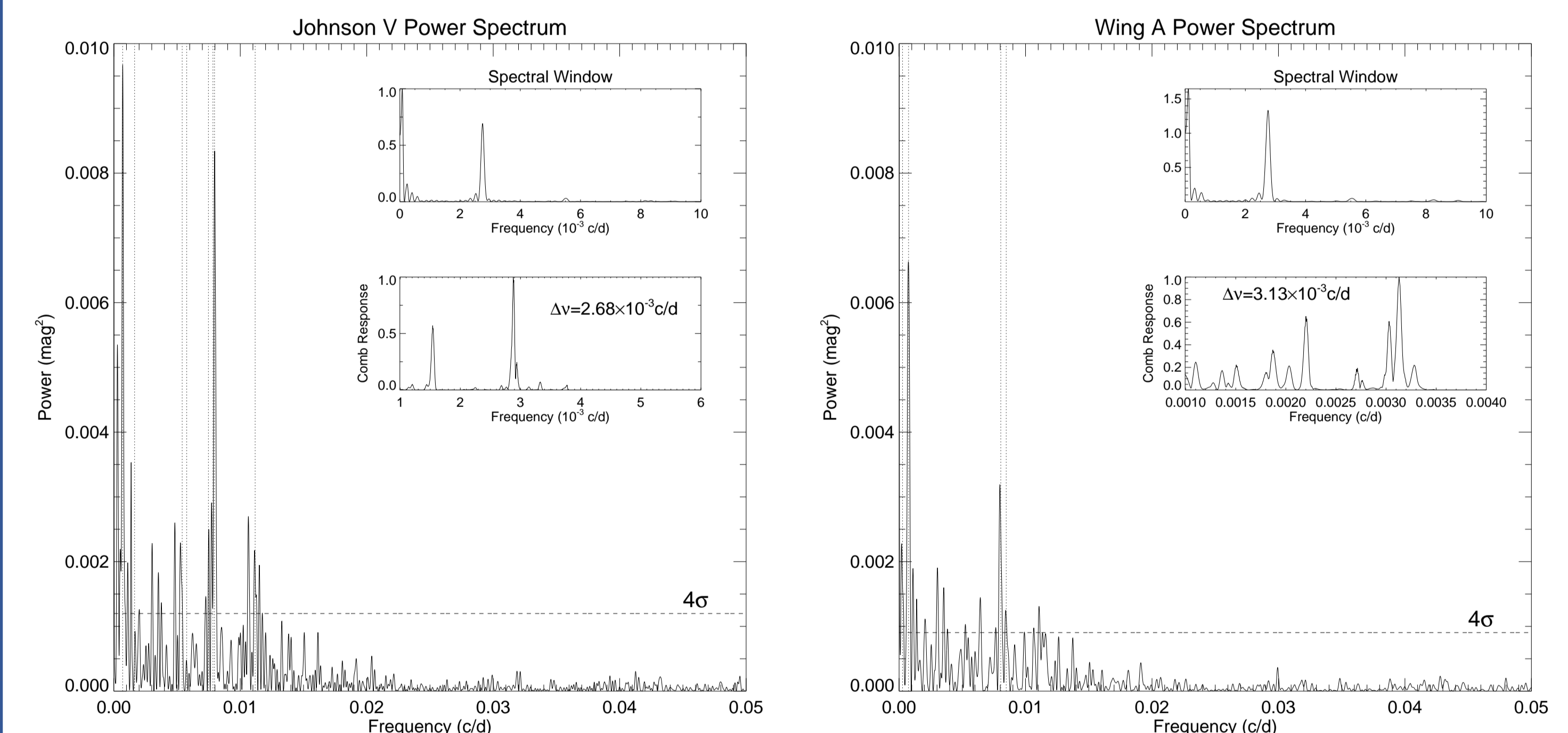


Scaling Mass and Radius From Asteroseismology

- Stochastically excited oscillations by turbulent convection is predicted in semi-regular pulsating stars [1]. Based on the large frequency spacing $\Delta\nu$ and the central frequency in the DFT hump ν_{max} , mass and radius scale as [3]

$$R/R_{\odot} = (\nu_{\text{max}}/\nu_{\text{max},\odot}) \cdot (\Delta\nu/\Delta\nu_{\odot})^{-2} \cdot (T_{\text{eff}}/T_{\odot})^{1/2}, \quad (1)$$

$$M/M_{\odot} = (R/R_{\odot})^3 \cdot (\Delta\nu/\Delta\nu_{\odot})^2. \quad (2)$$



- $\overline{\Delta\nu} = 0.22 \times 10^{-3}$ and $\nu_{\text{max}} \simeq 0.080 \text{ cd}^{-1}$ yield $M = 2.9 \pm 1.8 M_{\odot}$.

Table 2. Summary of α^1 Her Mass (m_1)

| $m_1 (M_{\odot})$ | Method | Remark |
|-------------------|-------------|---|
| 4.4 ± 1.3 | $\log g$ | Mean radii used is $286 \pm 31 R_{\odot}$ [5], but from Eq. 2 is $355 \pm 58 R_{\odot}$, |
| 2.9 ± 1.8 | $\Delta\nu$ | From Eq. 3 with mean radii from Eq. 2 (see above), |
| 2.1 to 3.0 | Isochrones | See Marigo et al. (2008) |
| | | Pulsation Prospective study , based on Xiong et al. (1998) |

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